

# MOTION CALCULATION



BY  
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DISTANCE  
DISPLACEMENT

s m

SPEED  
VELOCITY

v m s<sup>-1</sup>

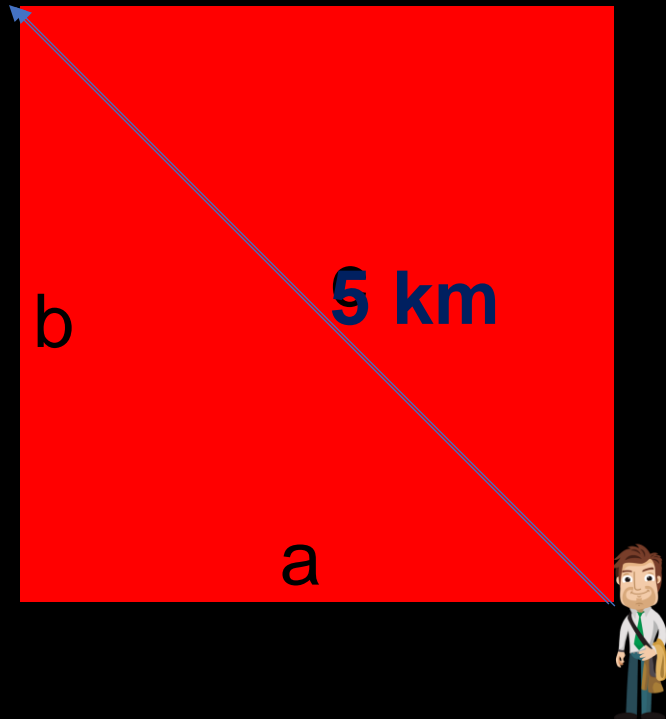
$$\frac{s}{t}$$

ACCELERATION

a m s<sup>-2</sup>

$$\frac{v-u}{t}$$

## EXAMPLE QUESTION 1



What's the distance and displacement?

**DISTANCE:**

$$3 + 4 = 7\text{km}$$

**DISPLACEMENT:**

$$3^2 + 4^2 = x^2$$

$$x = \sqrt{(3^2 + 4^2)}$$

$$x = \sqrt{(9 + 16)}$$

$$x = \sqrt{(25)}$$

$$x = 5$$

**PYTHAGORAS THEOREM:**

$$a^2 + b^2 = c^2$$

## EXAMPLE QUESTION 2



$$a = \frac{v - u}{t}$$

$$u = 1 \text{ ms}^{-1} \quad v = 0 \text{ ms}^{-1} \quad t = 5 \text{ s}$$

I walk at a uniform speed of  $1 \text{ ms}^{-1}$  before coming to stop in 5 seconds. What is my deceleration?

## EXAMPLE QUESTION 2



I walk at a uniform speed of  $1 \text{ ms}^{-1}$  before coming to stop in 5 seconds. What is my deceleration?

$$a = \frac{v - u}{t}$$

$$u = 1 \text{ ms}^{-1} \quad v = 0 \text{ ms}^{-1} \quad 5 \text{ s}$$

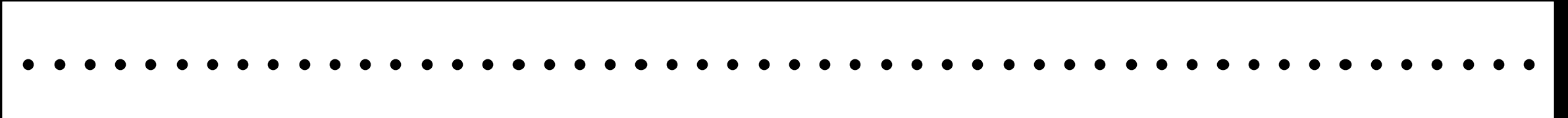
$$a = \frac{0 \text{ ms}^{-1} - 1 \text{ ms}^{-1}}{5 \text{ s}}$$

$$a = -0.1/5$$

$$a = -0.02 \text{ ms}^{-2}$$

# TICKER TIMER

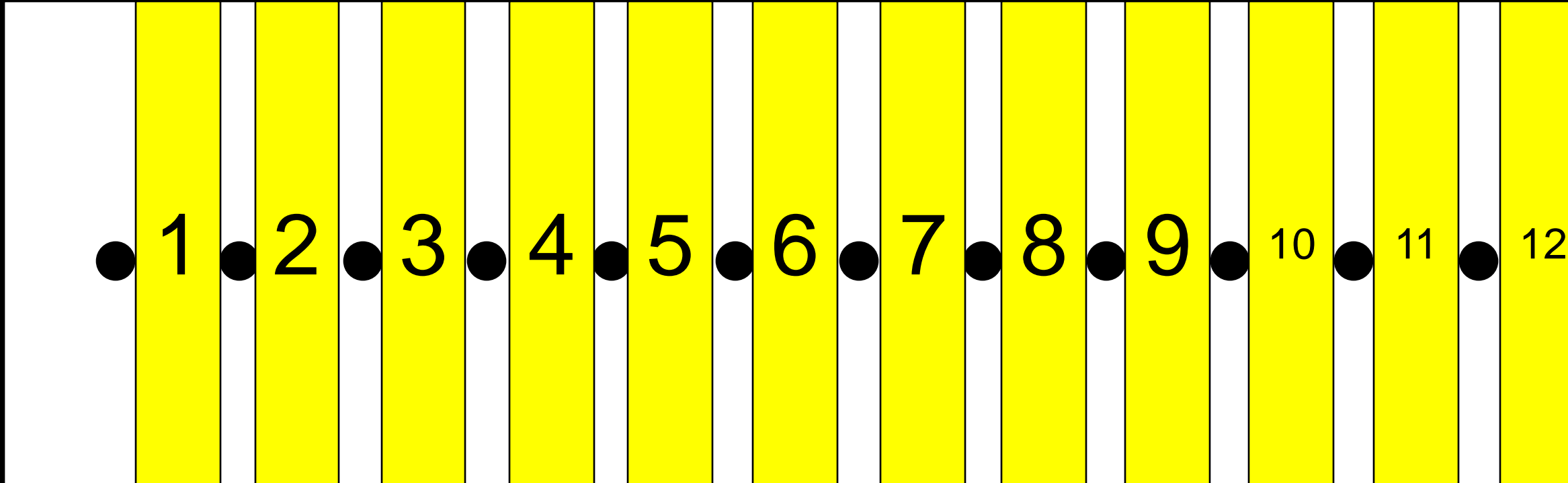
50hz (a.c. supply)



**50 tick**

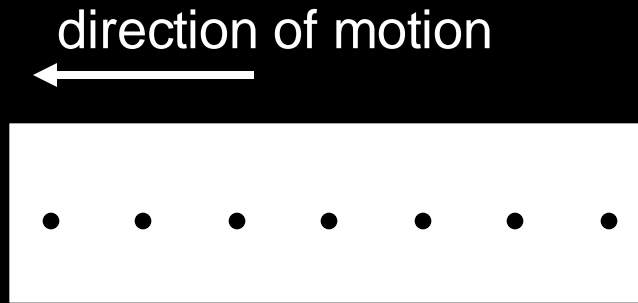
# TICKER TIMER

50hz (a.c. supply)

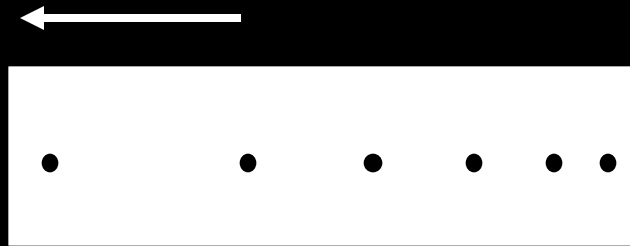


**50 tick = 50 dot-space**

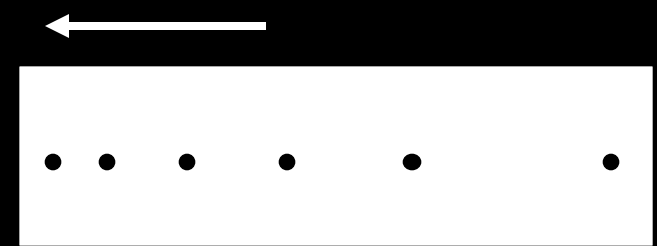
# TICKER TIMER



constant  
velocity



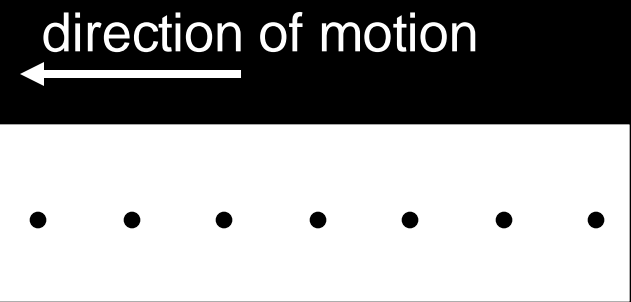
decelerates



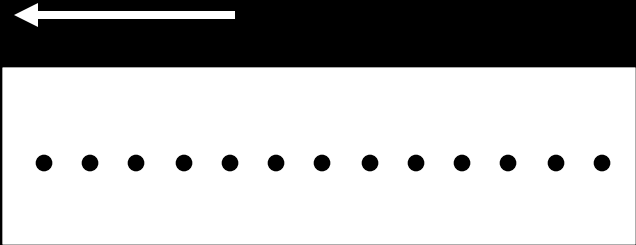
accelerates



**TICKER TIMER**



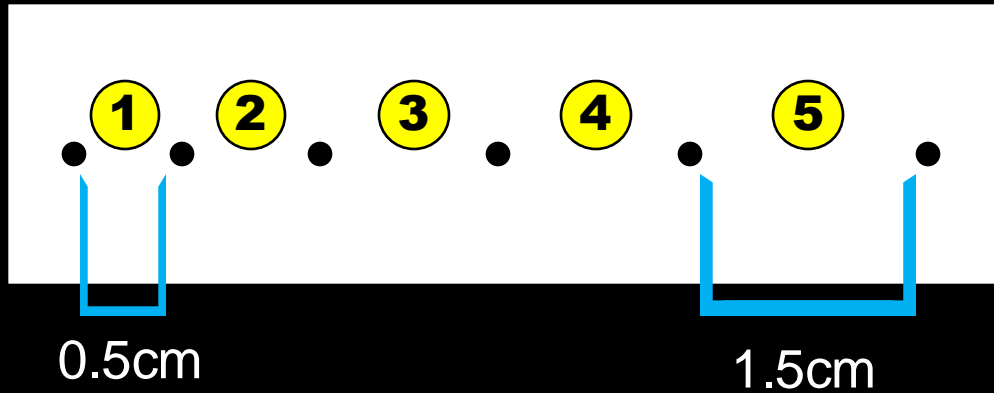
faster



slower

## EXAMPLE QUESTION 1

direction of motion  
←



Calculate the acceleration.

$$v = \frac{s}{t} \quad a = \frac{v-u}{t}$$

INITIAL VELOCITY

$$u = \frac{0.5}{0.02}$$

$$u = 25 \text{ cm s}^{-1}$$

FINAL VELOCITY

$$v = \frac{1.5}{0.02}$$

$$v = 75 \text{ cm s}^{-1}$$

TIME TAKEN

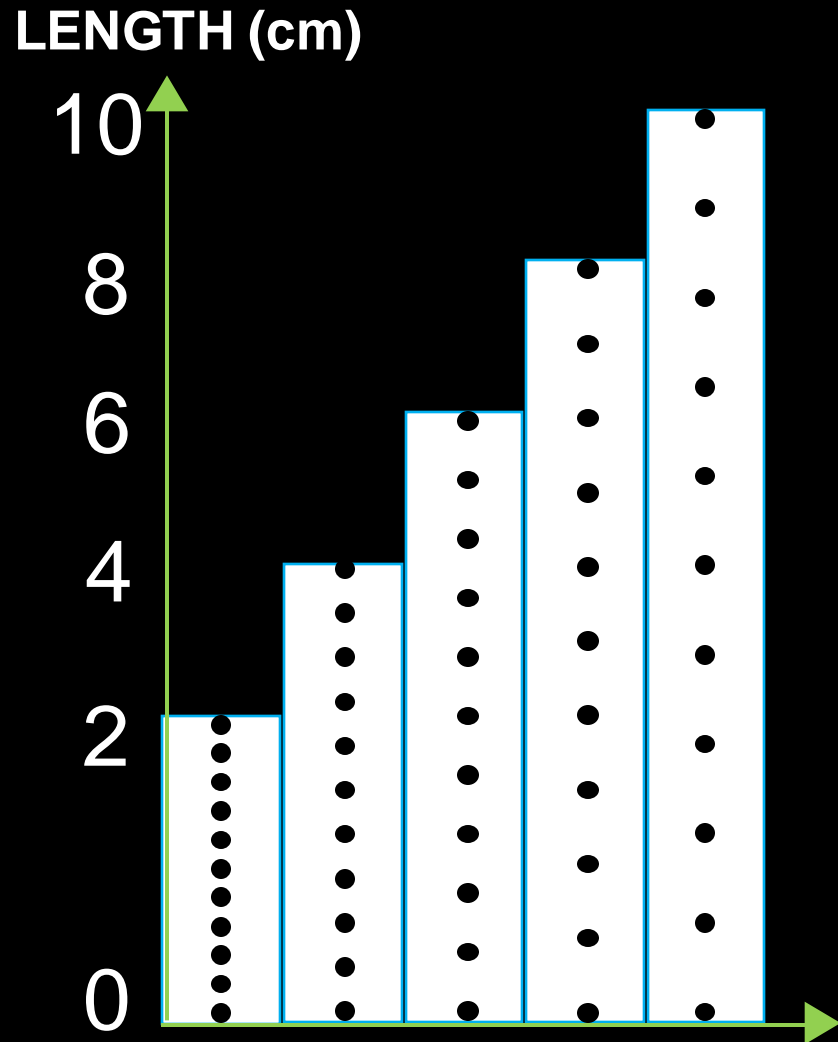
$$0.02 \times 5 = 0.1 \text{ s}$$

ACCELERATION

$$a = \frac{75-25}{0.1}$$

$$a = 500 \text{ cm s}^{-2}$$

## EXAMPLE QUESTION 2

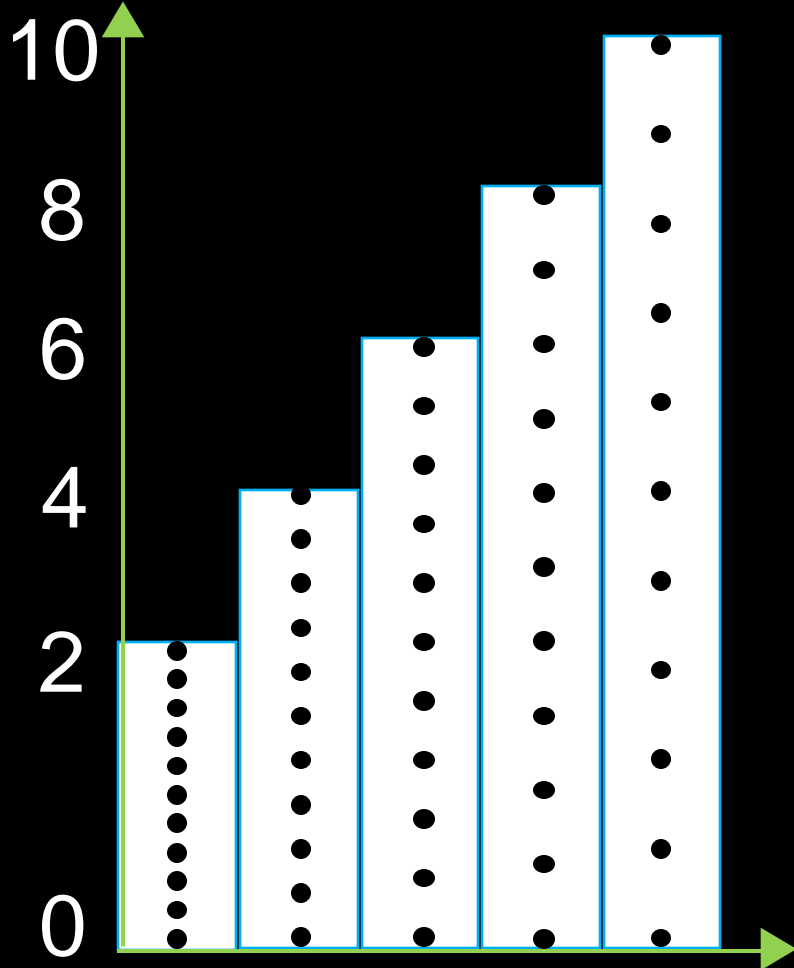


**Calculate the**

- a) total distance travelled
- b) total time taken
- c) average velocity
- d) acceleration

## EXAMPLE QUESTION 2

LENGTH (cm)



Calculate the

**total distance travelled**

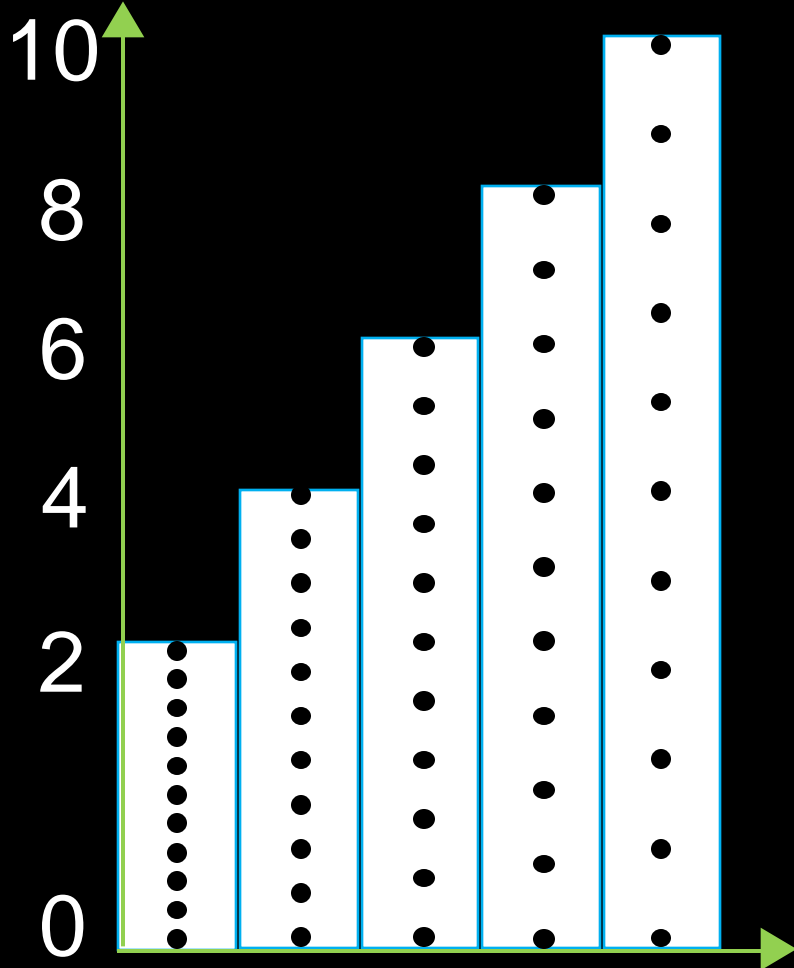
- b) total time taken
- c) average velocity
- d) acceleration

**TOTAL DISTANCE TRAVELLED**

$$2+4+6+8+10 = 30\text{cm}$$

## EXAMPLE QUESTION 2

LENGTH (cm)



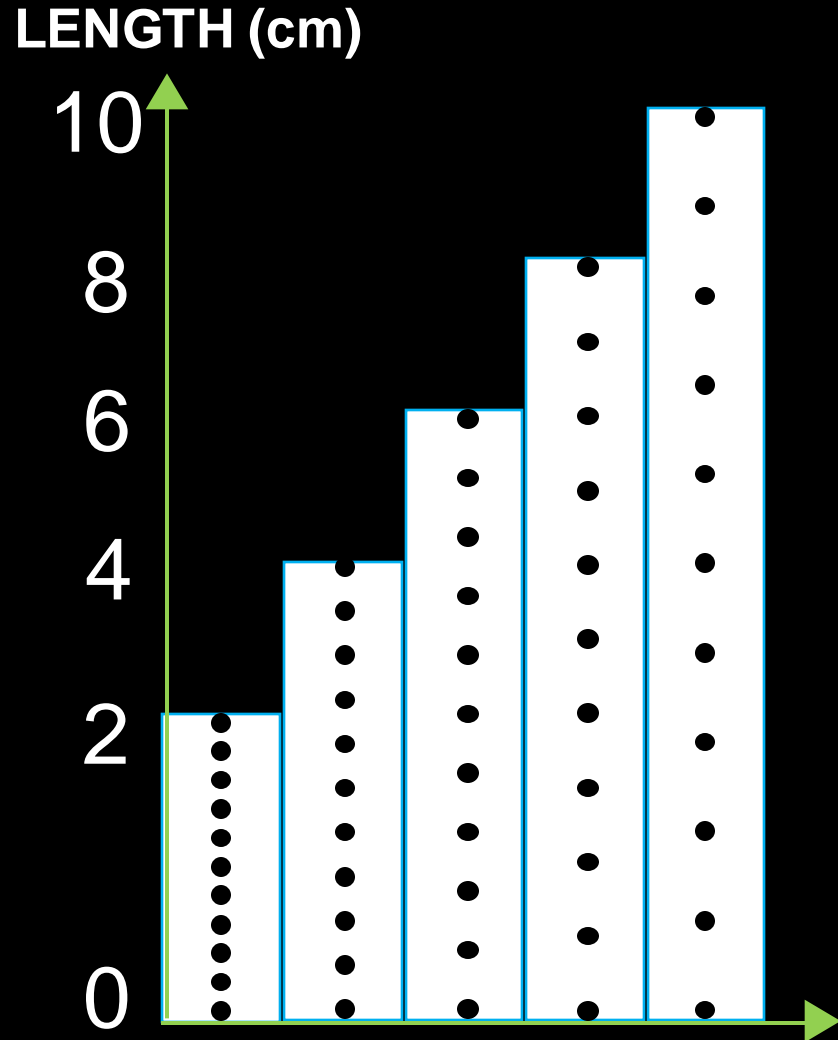
Calculate the

- a) total distance travelled
- b) total time taken
- c) average velocity
- d) acceleration

**TOTAL TIME TAKEN**

$$\begin{aligned} &0.02 \times (5 \times 10) \\ &= 0.02 \times 50 \\ &= 1 \text{ s} \end{aligned}$$

## EXAMPLE QUESTION 2



Calculate the

- a) total distance travelled
- b) total time taken
- c) average velocity
- d) acceleration

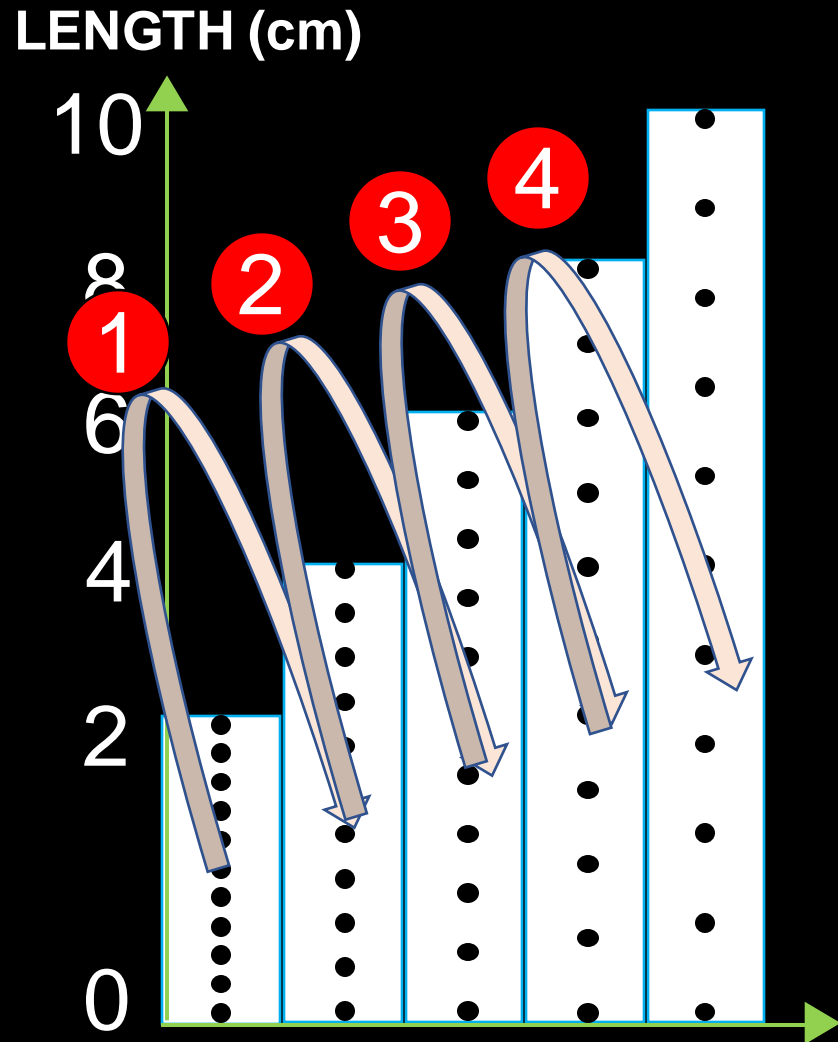
### AVERAGE VELOCITY

$$v = \frac{s}{t}$$

$$v = \frac{30\text{cm}}{1\text{s}}$$

$$v = 30 \text{ cm s}^{-1}$$

## EXAMPLE QUESTION 2



Calculate the

- a) total distance travelled
- b) total time taken
- c) average velocity
- acceleration

$$a = \frac{v - u}{t}$$

### ACCELERATION

$$v = 50 \quad u = 10 \quad t = 0.8$$

$$v = \frac{t}{a} = \frac{40 \text{ cm}}{0.02 \text{ s}} \times 4$$

$$a = 50 \text{ cm s}^{-1}$$

## EQUATIONS OF LINEAR MOTION

$$v = u + at$$

$$s = \frac{1}{2} (u+v)t$$

$$s = ut + \frac{1}{2} at^2$$

$$v^2 = u^2 + 2as$$

s= displacement

u= initial velocity

v= final velocity

a= uniform velocity

t= time interval



## EXAMPLE QUESTION 1



A car accelerates from  $20 \text{ m s}^{-1}$  with an acceleration of  $2 \text{ m s}^{-2}$ .

What is the **velocity** after **8 seconds**?

$$u = 20 \text{ m s}^{-1}$$

$$a = 2 \text{ m s}^{-2}$$

$$t = 8 \text{ s}$$

$$v = ?$$

$$v = u + at$$

$$v = 20 + 2(8)$$

$$v = 20 + 16$$

$$v = 36 \text{ m s}^{-1}$$

$$v^2 = u^2 + 2as$$

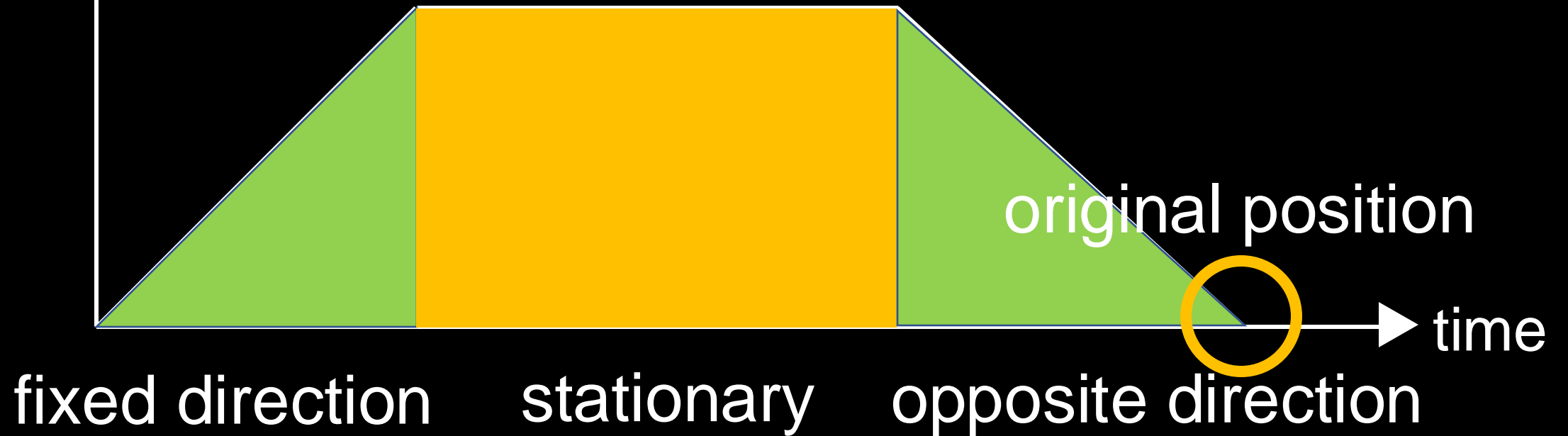
# MOTION GRAPH

## ST GRAPH

displacement

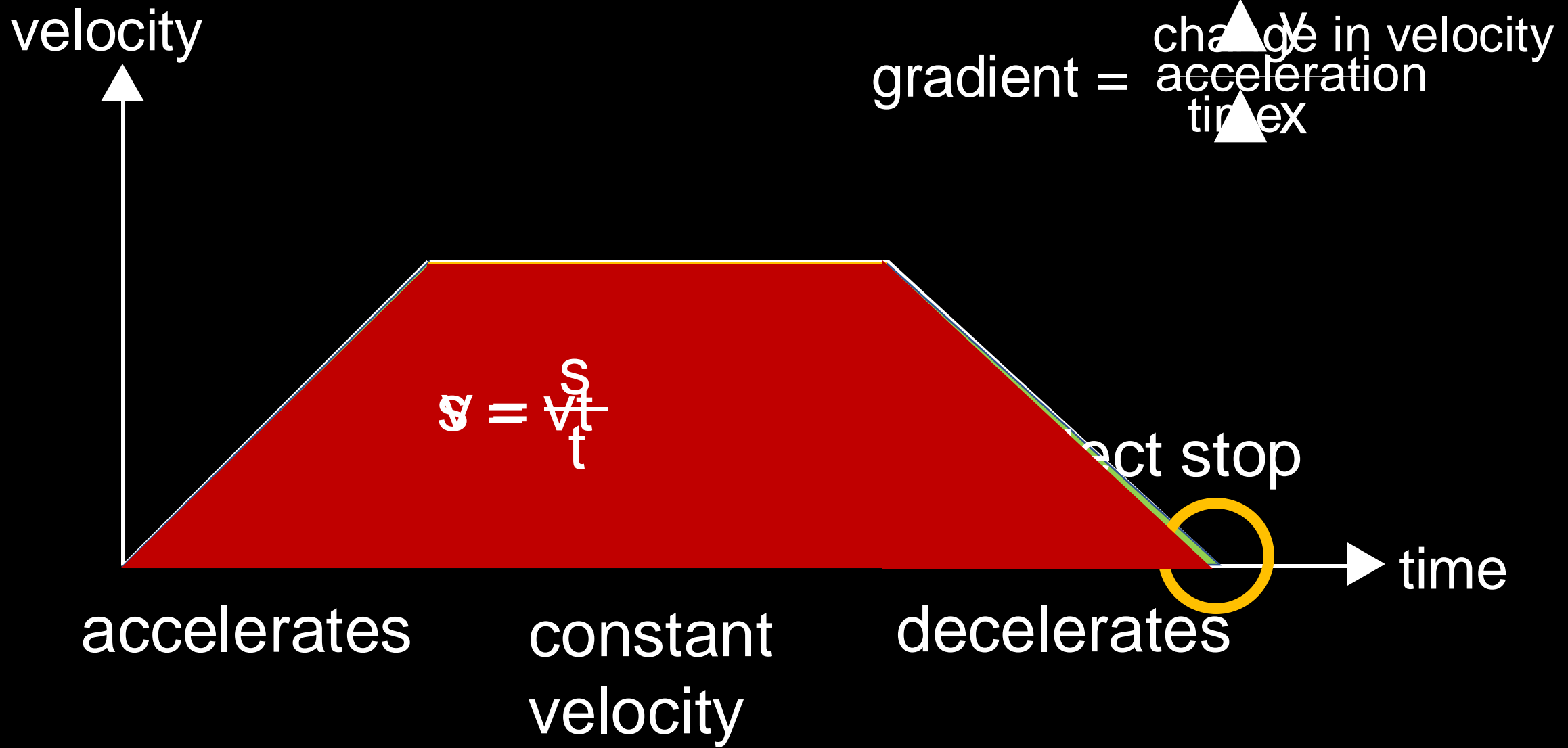
$$\text{gradient} = \frac{\text{displacement}}{\text{time}}$$

$\frac{v_2 - v_1}{t_2 - t_1}$



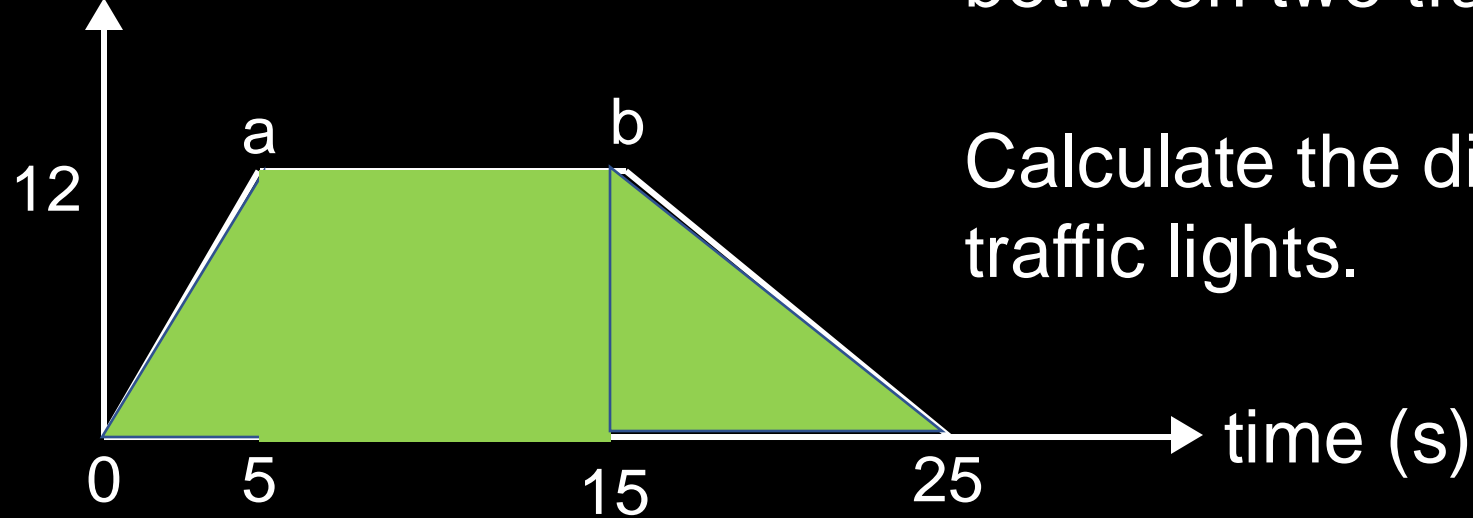
# MOTION GRAPH

## VT GRAPH



## EXAMPLE QUESTION 1

velocity ( $\text{m s}^{-1}$ )



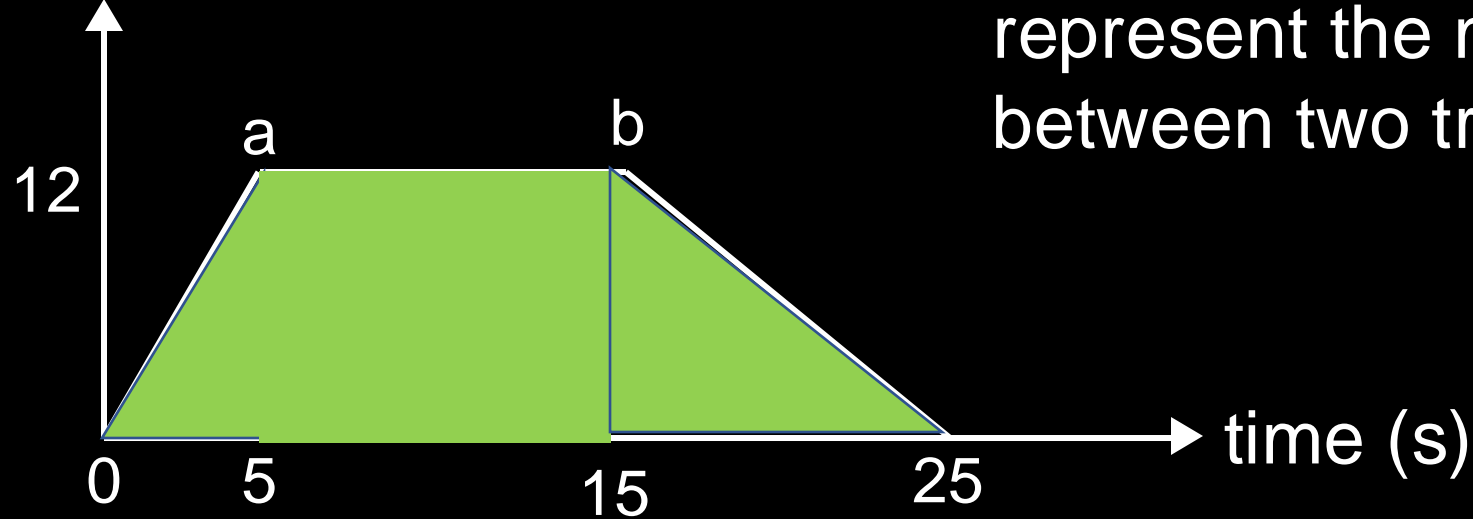
A motorcycle is travelling along the road between two traffic lights.

Calculate the distance between the two traffic lights.

$$\frac{12 \times 5}{2} = 30 \quad 10 \times 12 = 120 \quad \frac{12 \times 10}{2} = 60 \quad 30 + 120 + 60 = 210 \text{ m}$$

## EXAMPLE QUESTION 2

velocity ( $\text{m s}^{-1}$ )



Sketch an acceleration-time graph to represent the motion of the motorcycle between two traffic lights

$$\frac{12-0}{5-0} = 2.4 \quad a = 0 \quad \frac{0-12}{25-15} = -1.2$$

**0s-5s**

$2.4 \text{ m s}^{-2}$

**5s-15s**

$0 \text{ m s}^{-2}$

**15s-25s**

$-1.2 \text{ m s}^{-2}$

## EXAMPLE QUESTION 2

**0s-5s**

$2.4 \text{ m s}^{-2}$

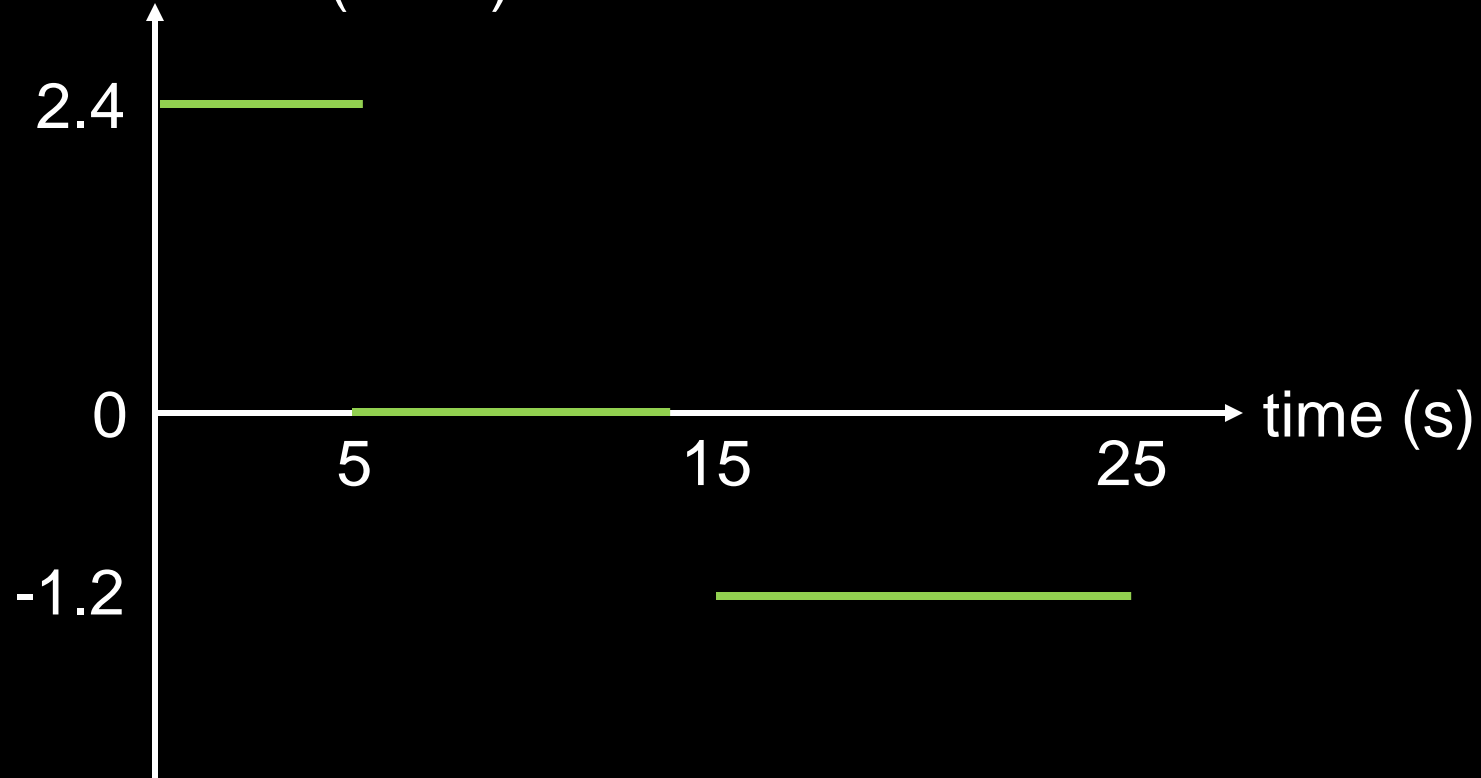
**5s-15s**

$0 \text{ m s}^{-2}$

**15s-25s**

$-1.2 \text{ m s}^{-2}$

acceleration ( $\text{m s}^{-2}$ )



# MOMENTUM

mass in motion

$$p = mv$$

## EXAMPLE QUESTION 1



A ball of mass 0.8kg strikes a wall at a velocity of  $10 \text{ m s}^{-1}$  and rebounds at  $6 \text{ m s}^{-1}$ .

What is the momentum before it strikes the wall?

$$p = mv$$

$$p = 0.8 \times 10$$

$$p = 8 \text{ kg m s}^{-1}$$



## EXAMPLE QUESTION 1



A ball of mass 0.8kg strikes a wall at a velocity of  $10 \text{ m s}^{-1}$  and rebounds at  $6 \text{ m s}^{-1}$ .

What is the momentum after the rebound?

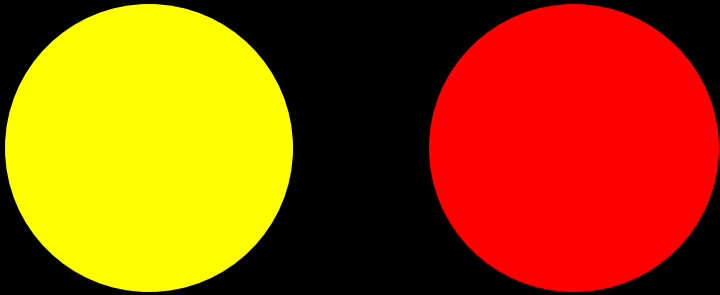
$$p = mv$$

$$p = 0.8 \times (-6)$$

$$p = -4.8 \text{ kg m s}^{-1}$$

# COLLISION

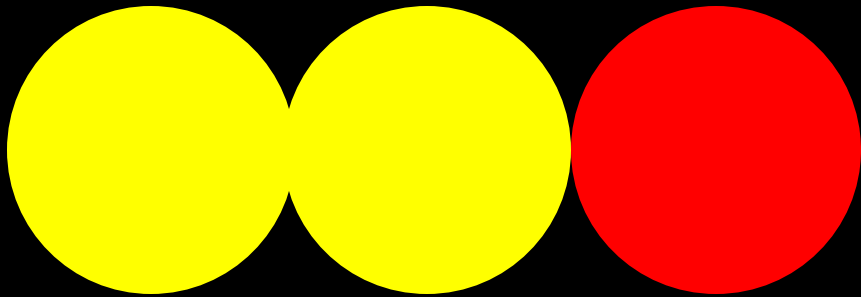
elastic



$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

# COLLISION

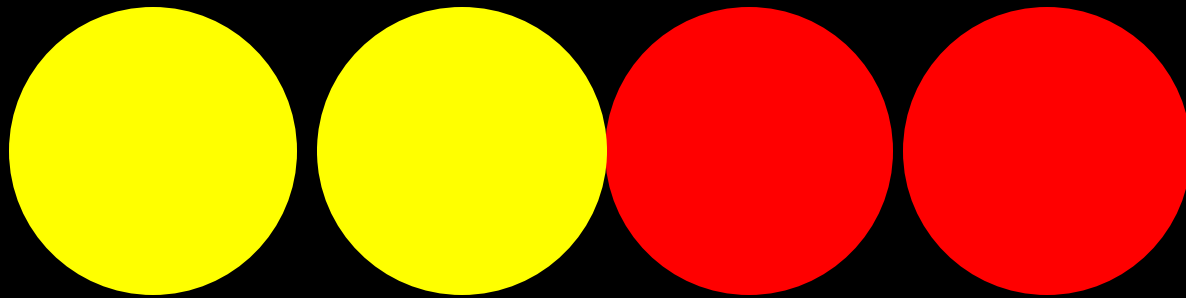
inelastic



$$m_1 u_1 + m_2 u_2 = (m_1 + m_2) v$$

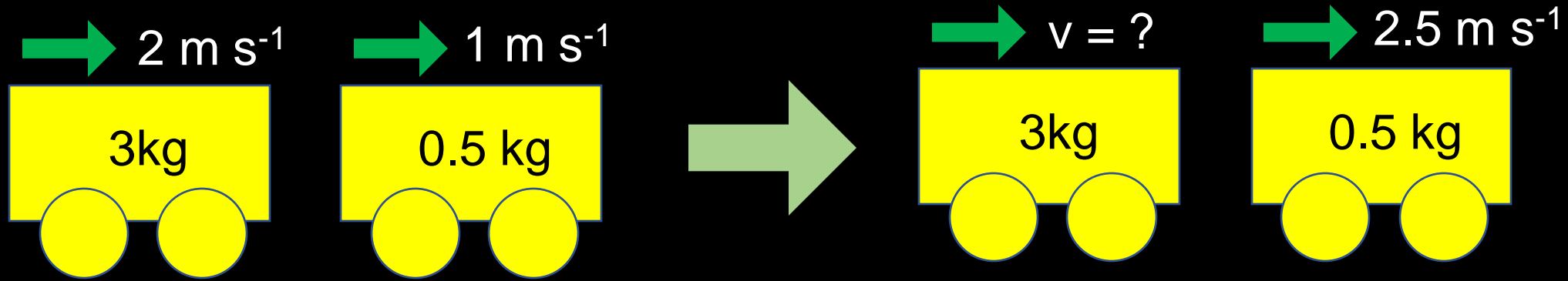
# COLLISION

explosion



$$m_1 u_1 + m_2 u_2 = 0$$

## EXAMPLE QUESTION 1



$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 u_2$$

$$3(2) + 0.5(1) = 3v + 0.5(2.5)$$

$$6.5 = 3v + 1.25$$

$$v = 1.75 \text{ m s}^{-1}$$



# THANK YOU

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